

# A Q-Factor Enhancement Technique for MMIC Inductors

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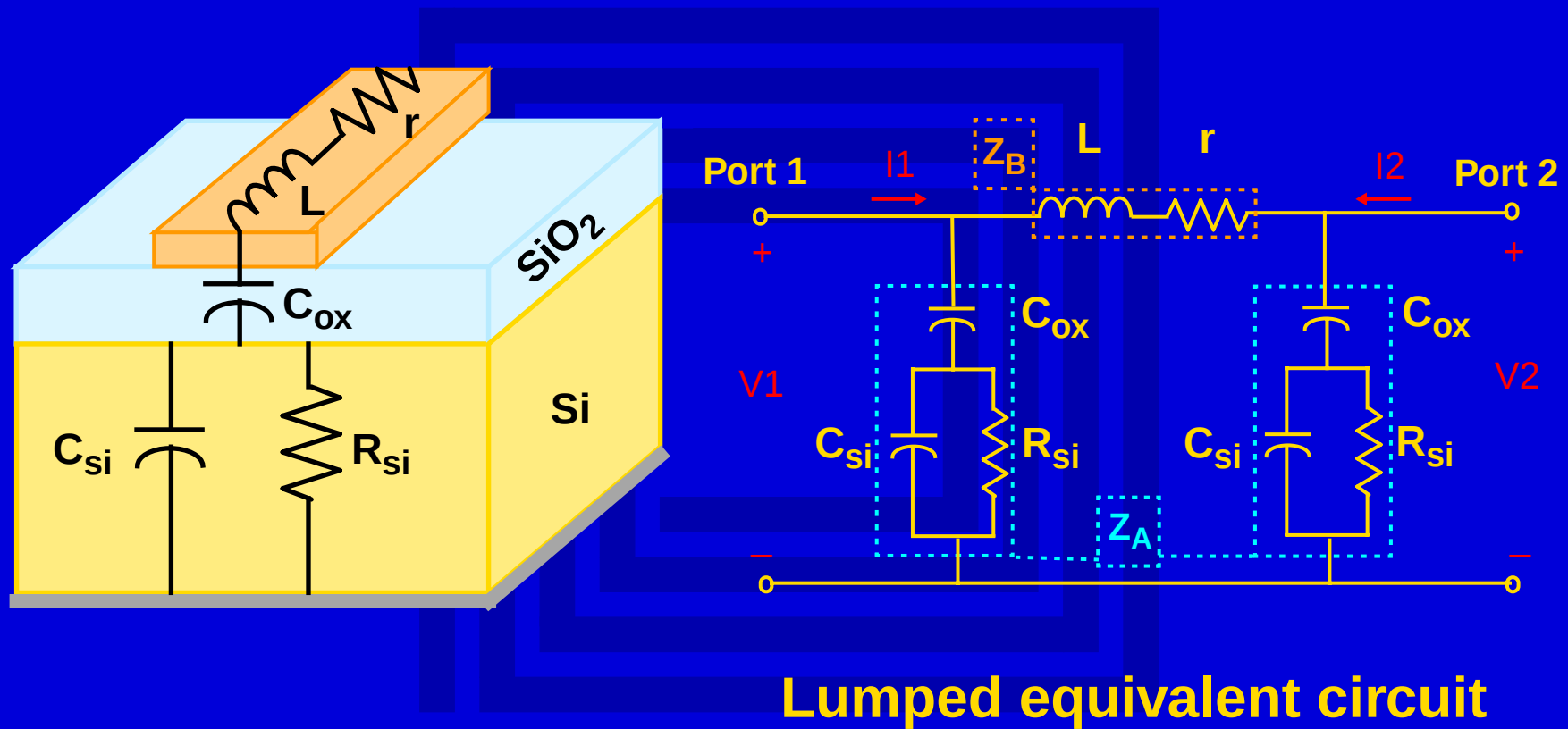


# Outline

- Introduction
- Differential excitation  
for higher Q-factor realization
- Symmetric spiral inductors
- Results
- Applications
- Conclusion



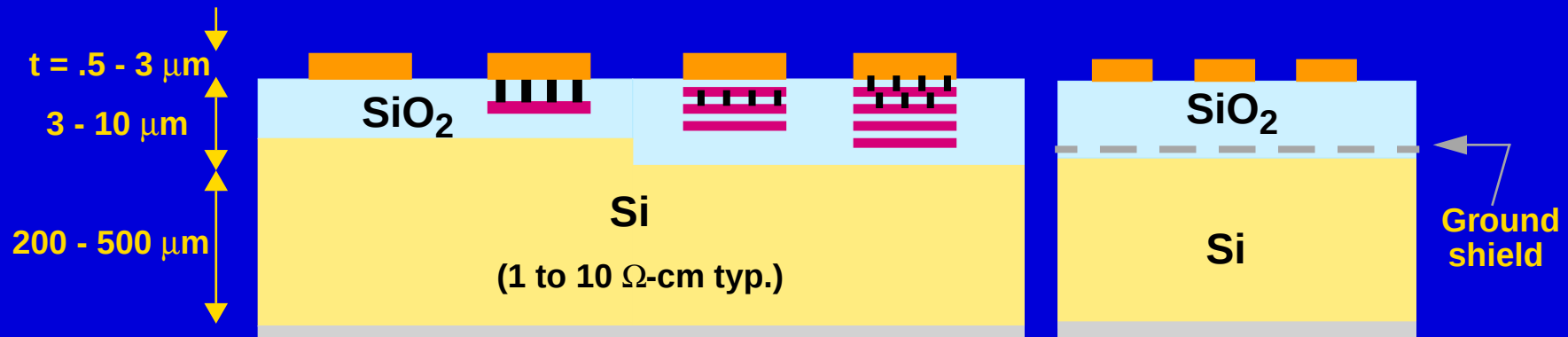
# Microstrip Line Modeling



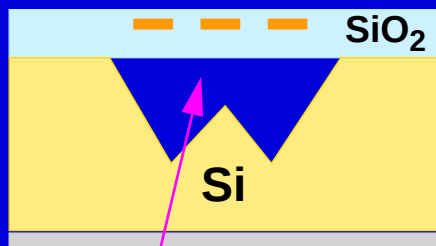
# Inductor Realizations in Si

MIS

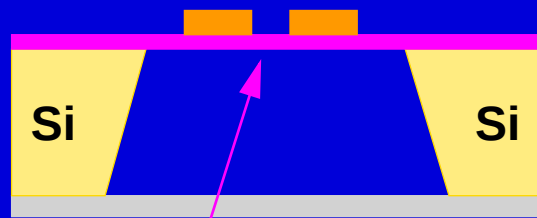
MIS + Ground shield



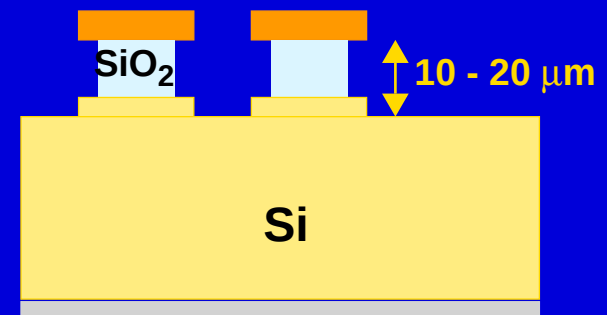
## Alternate structures



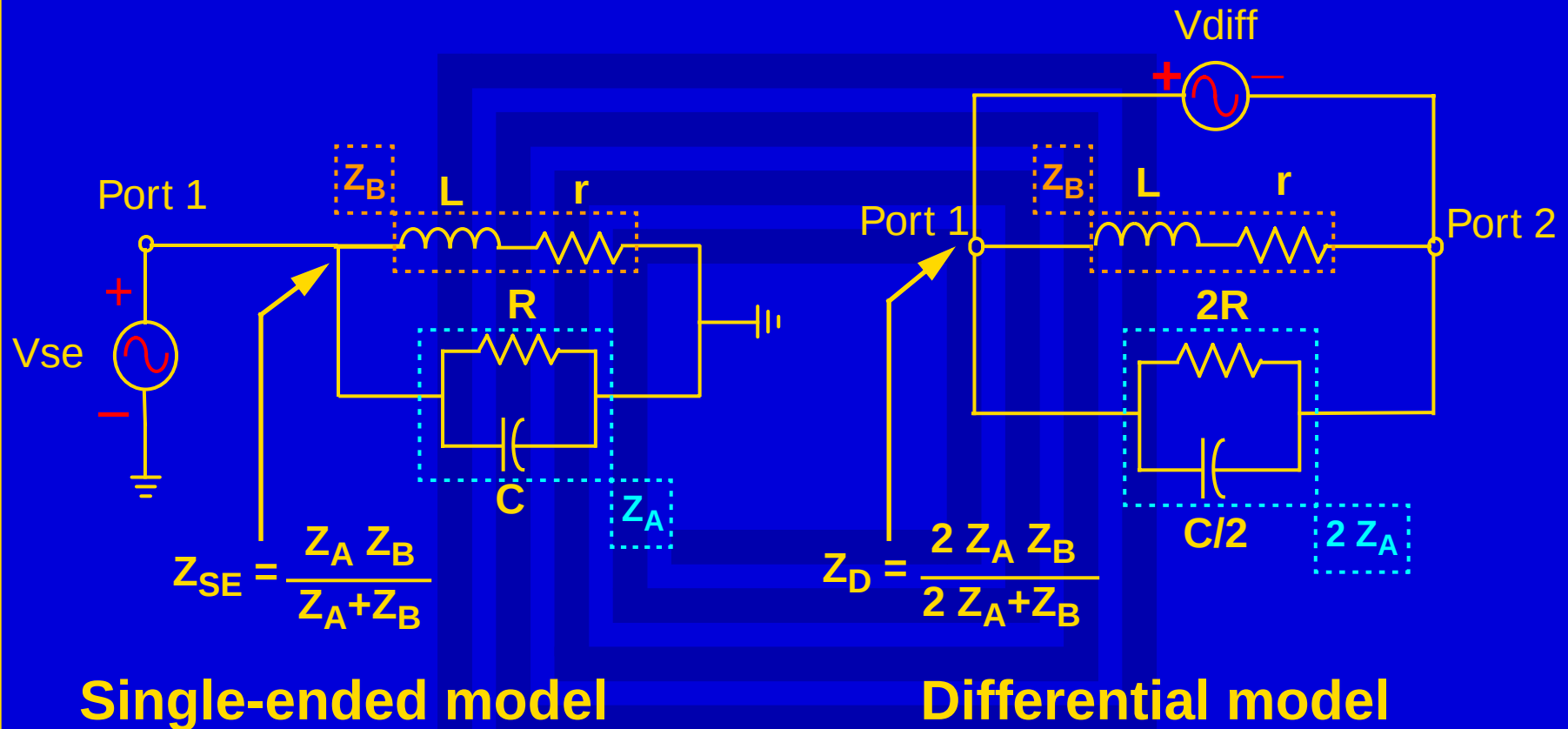
Etched cavity



Thin Membrane



# Single-ended / Differential Excitation



# Quality Factor

Below first resonant frequency of inductor

$$Q = \frac{2\pi fL}{\text{Re}[Z_{\text{input}}]}$$

- Low frequencies (<1 GHz)

$$Z_{\text{differential}} \approx Z_{\text{single-ended}}$$

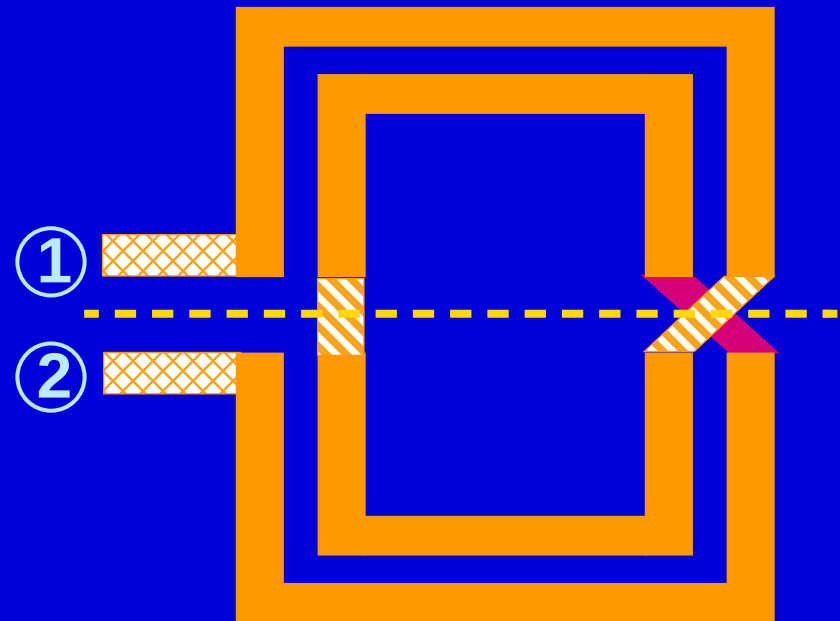
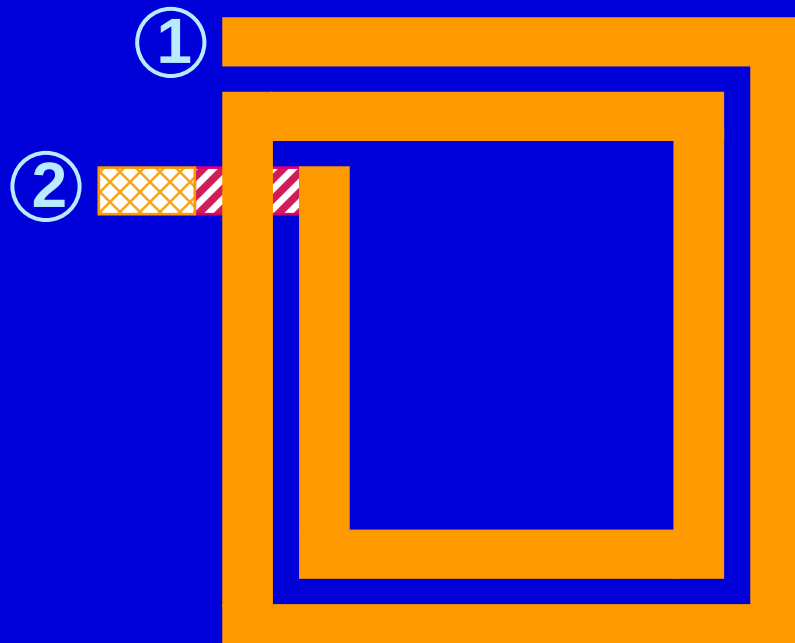
- Higher frequencies: increasing influence of substrate parasitics

$$\text{Re}[Z_{\text{differential}}] < \text{Re}[Z_{\text{single-ended}}]$$

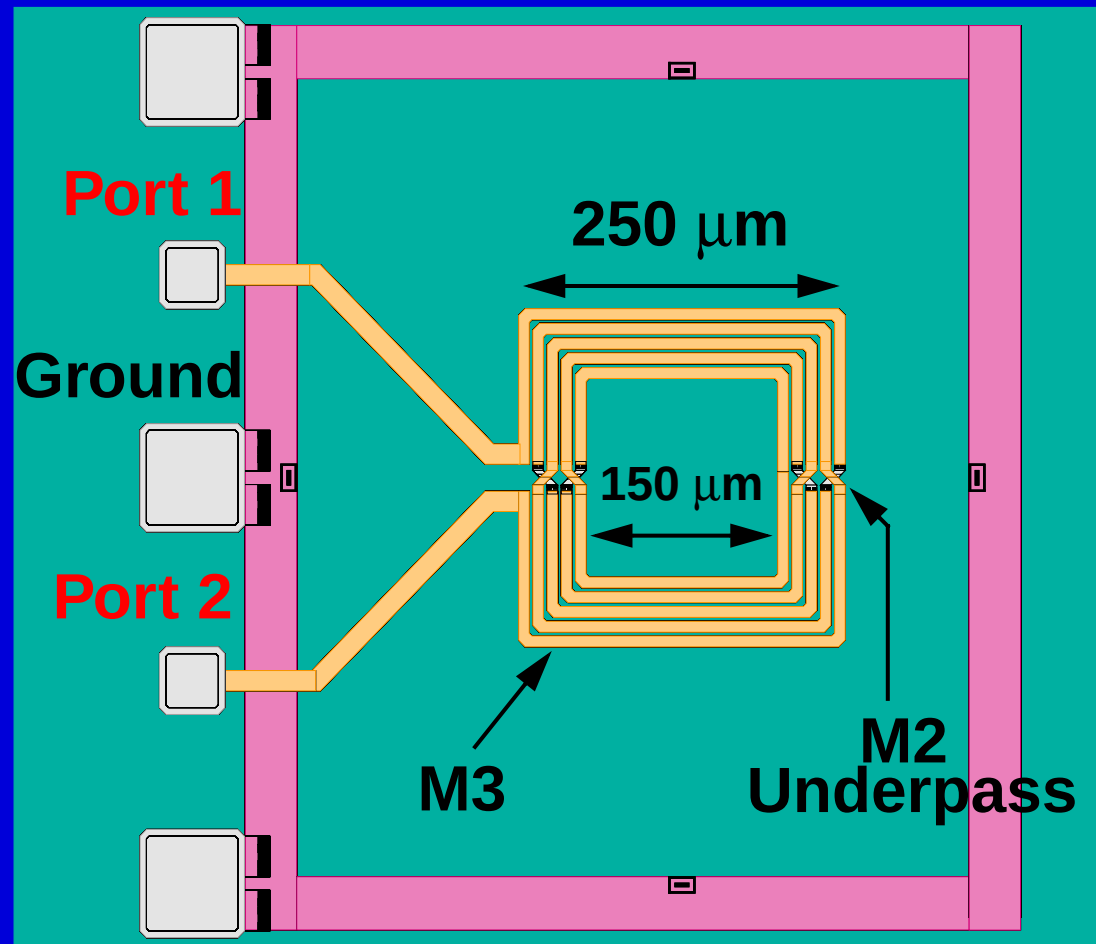
**Differential excitation: Higher Q and broader bandwidth**



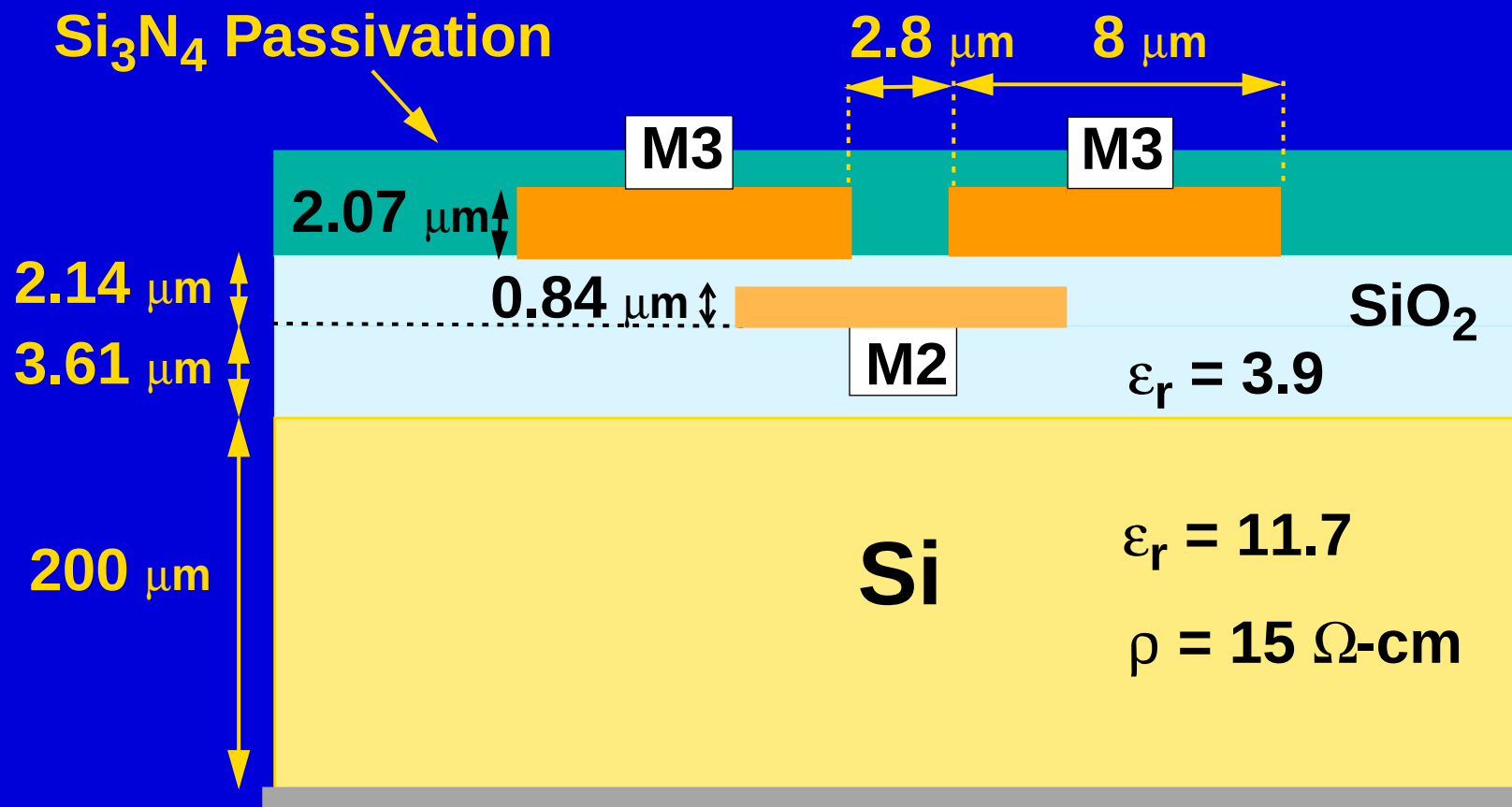
# Asymmetrical vs Symmetrical



# Symmetrical Spiral Inductor



# Technology



# Simulation / Measurement

- Full-wave EM simulation

- Measurement

## 2-port calibration:

- Probes on opposing sides for thru calibration
- Probes moved to same side for measurement

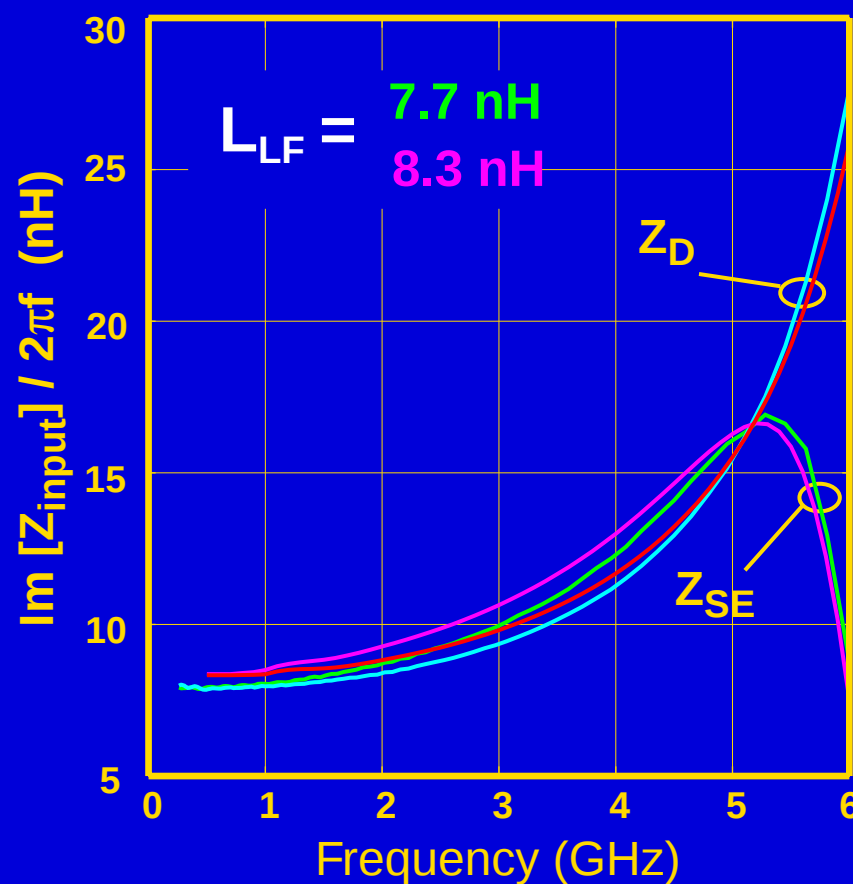
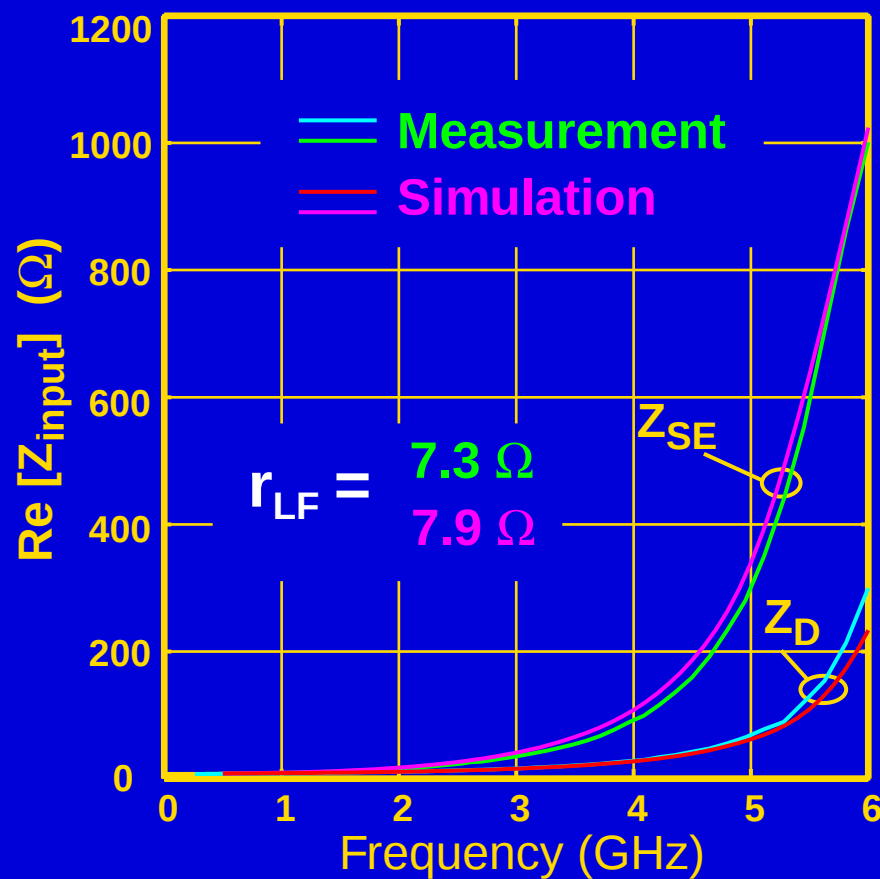
## De-embedding: Open / Short

- Differential:  $S_D = S_{11} - S_{21}$

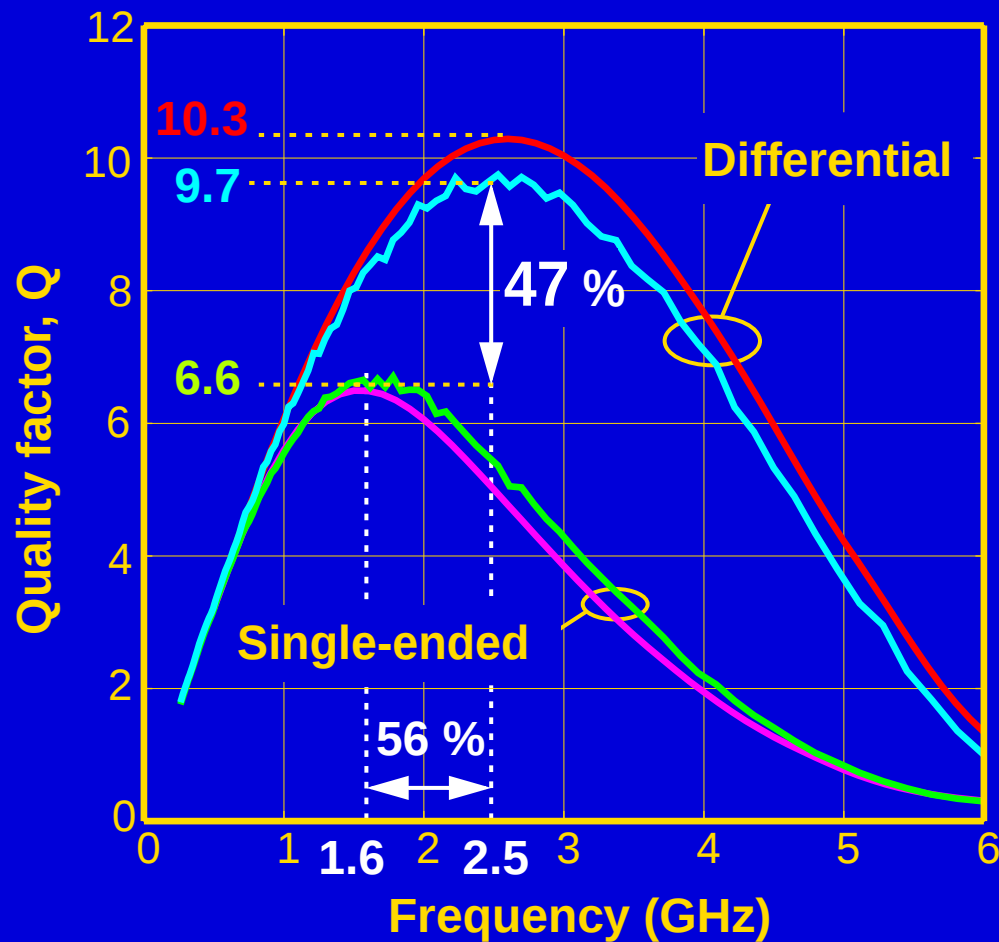
Input impedance:  $Z_D = Z_0 \left( \frac{1 + S_D}{1 - S_D} \right)$  ( $Z_0 = 100 \Omega$ )



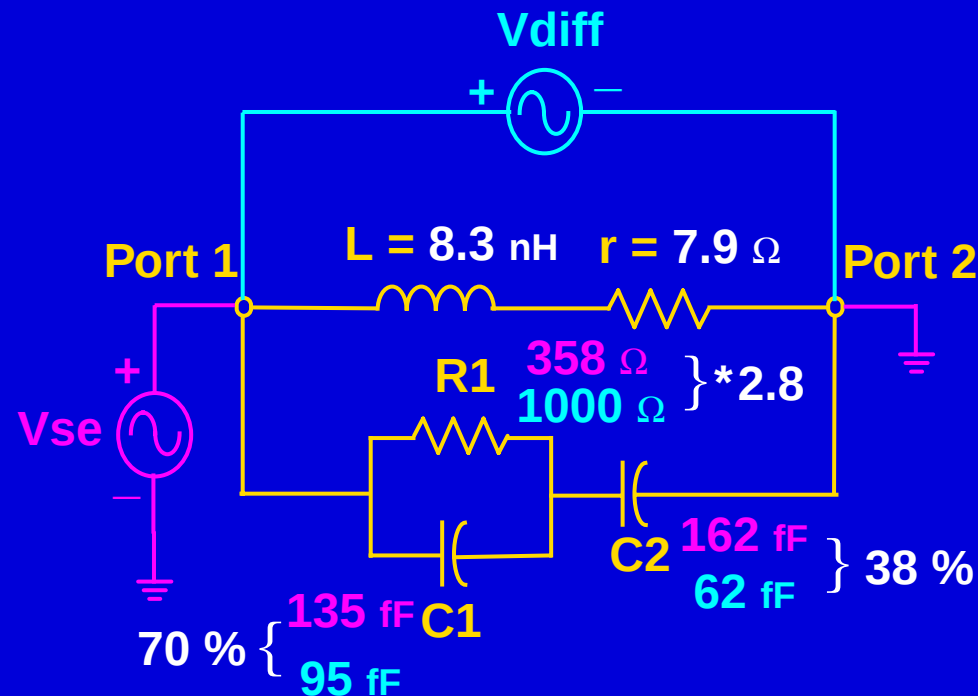
# Input Impedance



# Quality factor



# Equivalent Circuit Model



**Broadband parameter fit  
(0.5 - 6 GHz)**



# Measurement Errors

- **Topmetal thickness**

$$t_{M3} + 10\% = 2.27 \mu\text{m} \longrightarrow r = 7.5 \Omega \text{ (Meas: } 7.3 \Omega \text{)}$$

- **NA accuracy:** connectors, cables, temperature, frequency drifts

- **Calibration**

- **De-embedding error**

Probe resistance ( $r = 0.3 \Omega$ )

Parasitics of open / short interconnects and pads

$$C = 63 \text{ fF @ } 2 \text{ GHz} / L = 250 \text{ pH, } r = 0.24 \Omega$$

- **Parameter variation**

Si resistivity

Layer thickness, width, spacing

Temperature

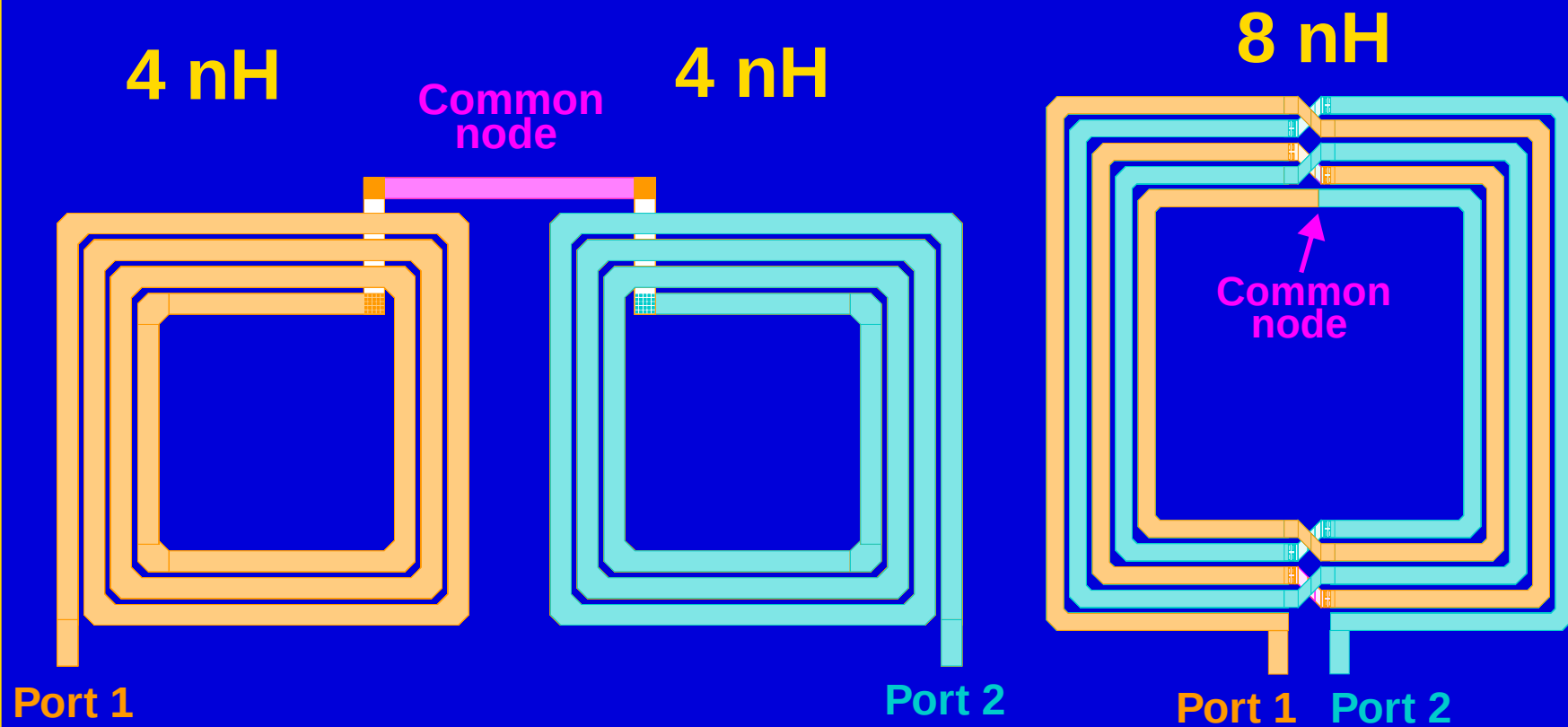


# Results

| Inductor type            | Reference   | Si $\rho$                | t ( $\mu\text{m}$ ) | L (nH)     | Q-factor                          |
|--------------------------|-------------|--------------------------|---------------------|------------|-----------------------------------|
| 1-level metal            | Long        | 10 $\Omega\text{-cm}$    | 1-3                 | 1.88       | 6-10 @ 4 GHz                      |
| 2-level metal            | Park        | 2 k $\Omega\text{-cm}$   | 2                   | 13         | 12 @ 3 GHz                        |
| 5-level metal            | Burghartz   | 12 $\Omega\text{-cm}$    | 4.3                 | 2.2        | 16 @ 2 GHz                        |
| Ground shield            | Yue         | 10-20 $\Omega\text{-cm}$ | 2                   | 8          | 7.2 @ 1.5 GHz                     |
| Membrane                 | Chi         | 2 k $\Omega\text{-cm}$   | 1 (Au)              | 0.9<br>1.2 | 20 @ 4.3 GHz<br>Res. freq: 70 GHz |
| Etched oxide/Si          | Rieh        | 10 k $\Omega\text{-cm}$  |                     | 2          | Res. freq: 30 GHz                 |
| Differential Symmetrical | Danesh Long | 15 $\Omega\text{-cm}$    | 2                   | 8          | 9.7 @ 2.5 GHz                     |



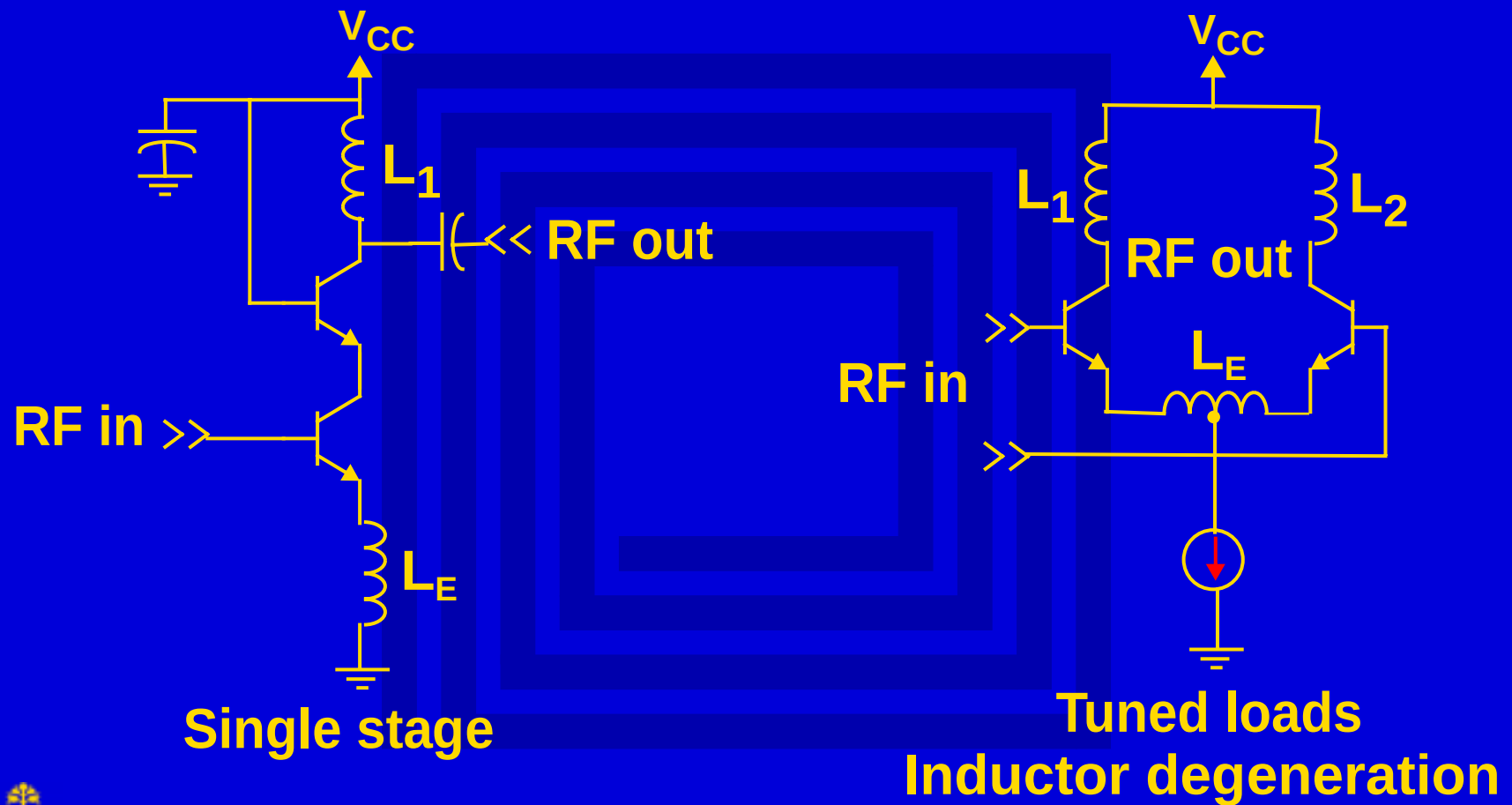
# Layout comparison



**Chip area reduction**



# Amplifier



# Conclusion

- **Differential vs single-ended excitation: lower parasitics**
  - Higher peak Q-factor (50% +)
  - Higher peak frequency (50% +)
  - Broader operating bandwidth
- **RF applications**
  - Symmetrical inductors (reduced chip area)
  - Oscillators, amplifiers, mixers ...
  - Other substrates: GaAs
- **Monolithic circuits: extra components have small marginal cost**

