

Full-Dimension MIMO Arrays with  
Large Spacings Between Elements

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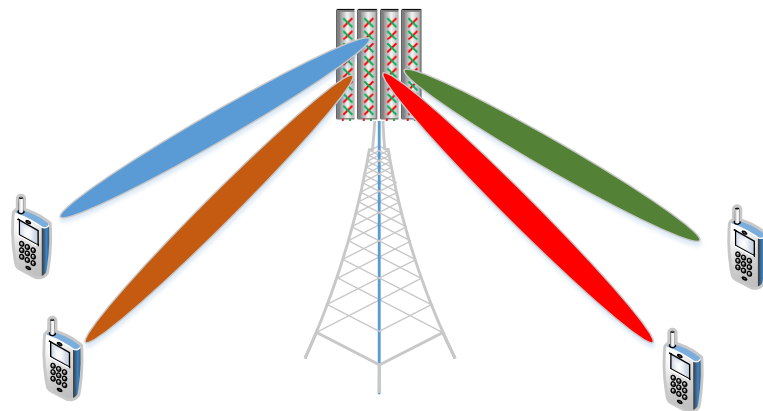
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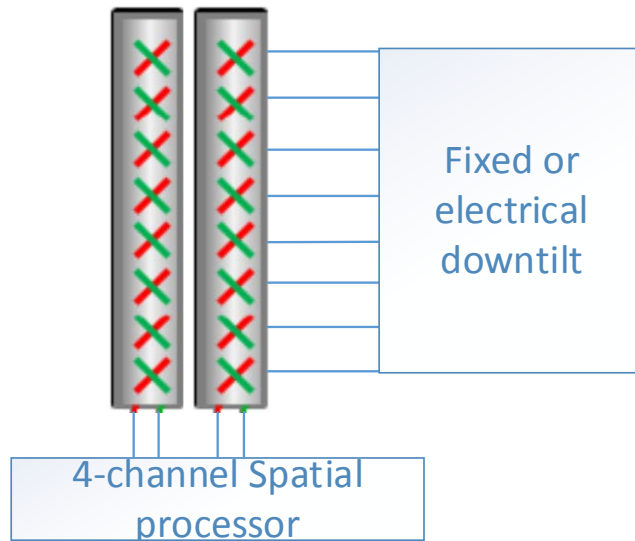
- Introduction to Massive MIMO and FD-MIMO
- Compact arrays with Kronecker channel model
- Linear arrays with spatial channel model (SCM)
- FD-arrays
- Conclusions

- Multiuser-MIMO using a number of BS antennas well in excess the number of active users.
- Benefits:
  - The effects of uncorrelated noise and fast fading vanish when the number of antennas increases without limit
  - In practice, array gains provide unprecedented capacity increase and/or transmission power save.
  - Simple linear precoding schemes such as MRT and ZF are near-optimal.
- Drawbacks:
  - In practice, hundreds of antennas are needed.
  - Implementation challenges related to cost, synchronization, channel estimation etc.
  - **A solution for accommodating very large number of antennas in constrained practical BS physical spaces is needed!!!**

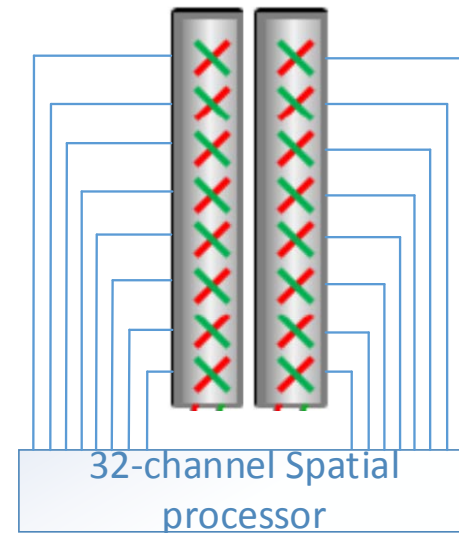


# Full dimension-MIMO

- Traditionally, vertical beamforming weights remain fixed for optimized coverage
- In FD-MIMO adaptive beamforming is performed in both azimuth and elevation dimensions
- FD-MIMO is an enabler for compact Massive MIMO antennas



Traditional MIMO



FD-MIMO

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- A base station equipped with an array of  $M$  antennas serving  $K$  single antenna user terminals (downlink transmission)
- Received signal:

$$\mathbf{x} = \mathbf{G}\mathbf{s} + \mathbf{w} \quad \text{with} \quad \mathbb{E}[\mathbf{w}\mathbf{w}^H] = \sigma_w^2 \mathbf{I}$$

- Two pre-coders are considered in transmission:

- Maximum ratio transmission (MRT):  $\mathbf{s} = \sqrt{\frac{P}{\text{trace}(\mathbf{G}\mathbf{G}^H)}} \mathbf{G}^H \mathbf{a}$

- Zero Forcer:  $\mathbf{s} = \sqrt{\frac{P}{\text{trace}((\mathbf{G}\mathbf{G}^H)^{-1})}} \mathbf{G}^H (\mathbf{G}\mathbf{G}^H)^{-1} \mathbf{a}$

with  $\mathbb{E}[\mathbf{s}^H \mathbf{s}] \leq P$

and  $\rho = \frac{P}{\sigma_w^2}$

Artiga, X.; Devillers, B.; Perruisseau-Carrier, J., "On the selection of radiating elements for compact indoor massive-multiple input multiple output base stations," *Microwaves, Antennas & Propagation, IET*, vol.8, no.1, pp.1,9, January 8 2014

- Assuming:
  - Uncorrelated fading processes at Tx and Rx
  - Uncorrelated user terminals
  - Uniform 3D-APS and lossless antennas at the BS side
- The channel matrix becomes:

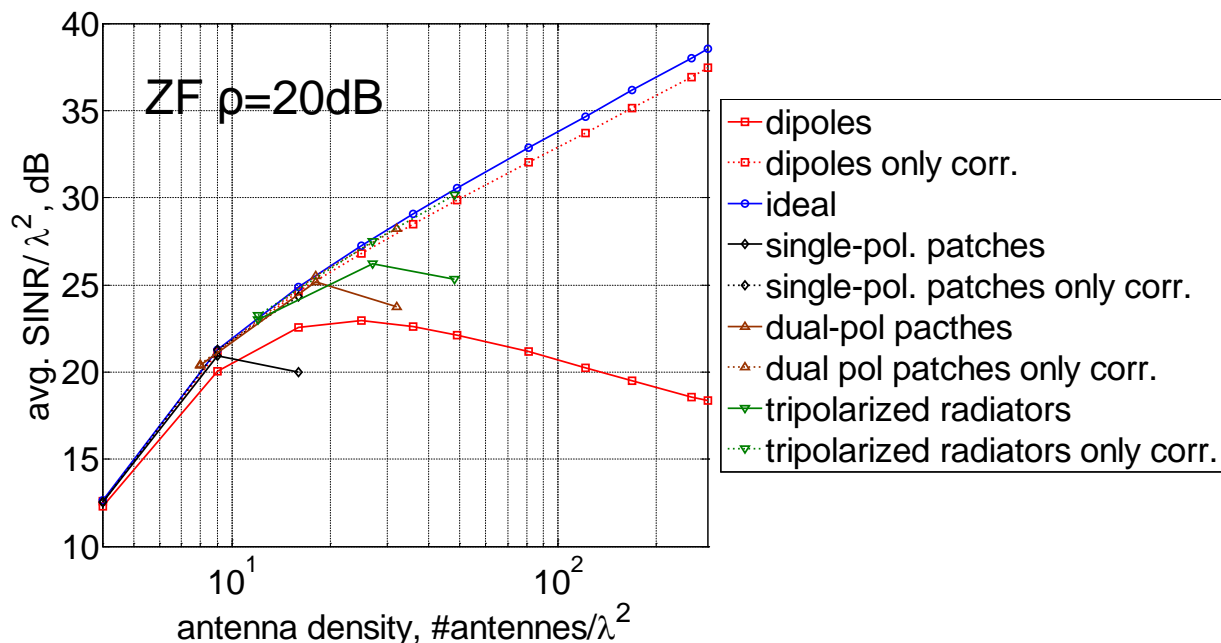
$$\mathbf{G} = \mathbf{H}(\mathbf{X}_T^{1/2})^T \quad \text{where } \mathbf{H}: \text{random matrix with Gaussian i.i.d. elements}$$

And  $\mathbf{X}_T$  is the Tx antennas covariance matrix:

$$\mathbf{X}_T = c(\mathbf{I} - \mathbf{S}_T \mathbf{S}_T^H) \quad \text{where } \mathbf{S}_T \text{ is the S-matrix of the Tx antenna system}$$

# Simulation results

- Average SINR per user is evaluated while increasing the number of antennas included in a physically constrained  $\lambda \times \lambda$  square array.
- $\mathbf{S}_T$  matrices are computed using ANSYS HFSS
- Single-port input impedance match and channel XPR=0dB are assumed
- $K=4$  uncorrelated users

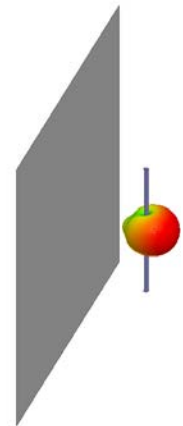
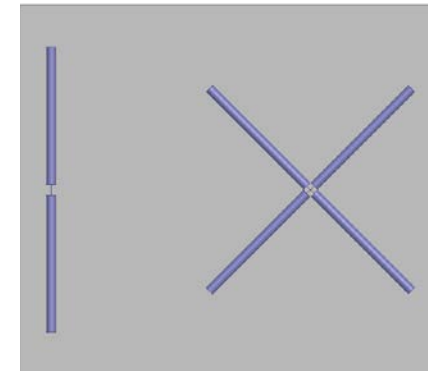
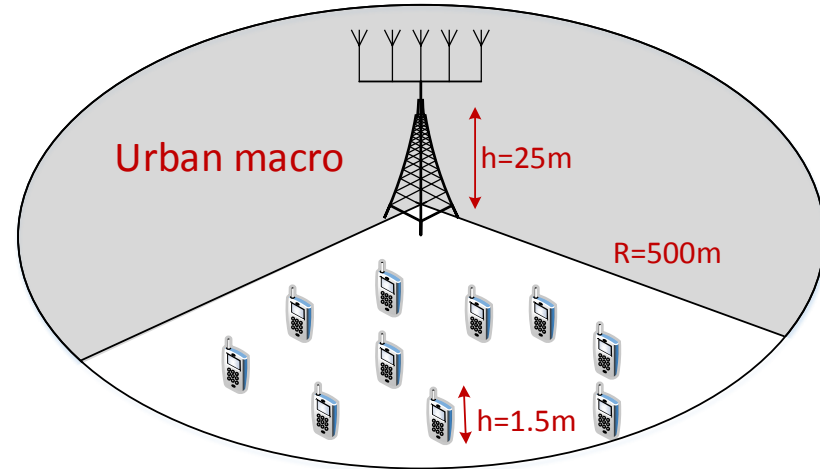


- An optimum antenna density is found regardless of the radiating element or the pre-coder
- Optimum inter-element distances are  $\lambda/4$  for dipoles and  $\lambda/2$  for patches
- Dual-polarized patches perform better than compact arrays of dipoles



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- **Linear arrays with spatial channel model (SCM)**
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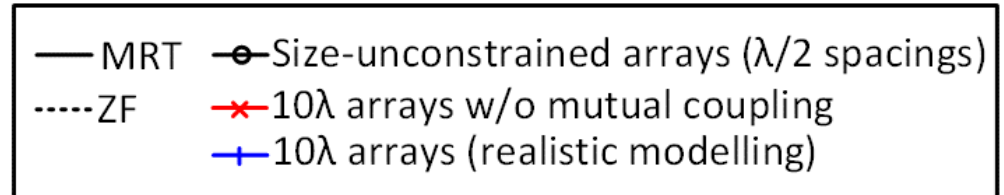
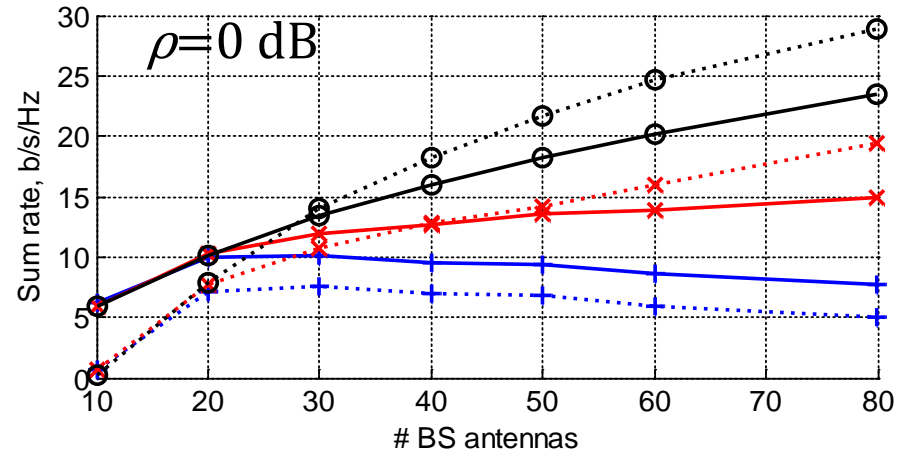
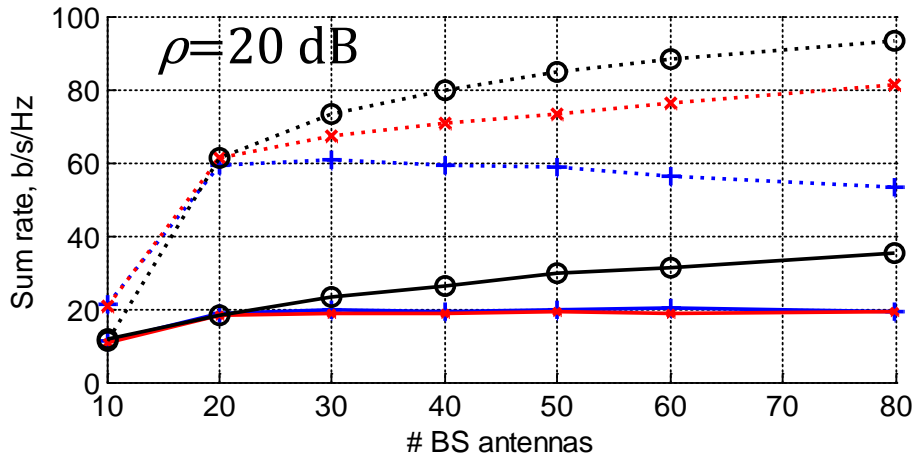
- Downlink transmission on a single 120° sector.
- $K=10$  uniformly distributed users
- Urban macro 3D spatial channel model based on WINNER+.
- Realistic antenna pattern simulation using HFSS (vertical or crossed-dipoles backed with PEC).
- Omnidirectional ideal antennas assumed for the user terminals.
- Uniform power allocation



Artiga, X.; Perruisseau-Carrier, J.; Perez-Neira, A.I., "Antenna array configurations for massive MIMO outdoor base stations," *Sensor Array and Multichannel Signal Processing Workshop (SAM), 2014 IEEE 8th*, vol., no., pp.281,284, 22-25 June 2014

- **Compact arrays**

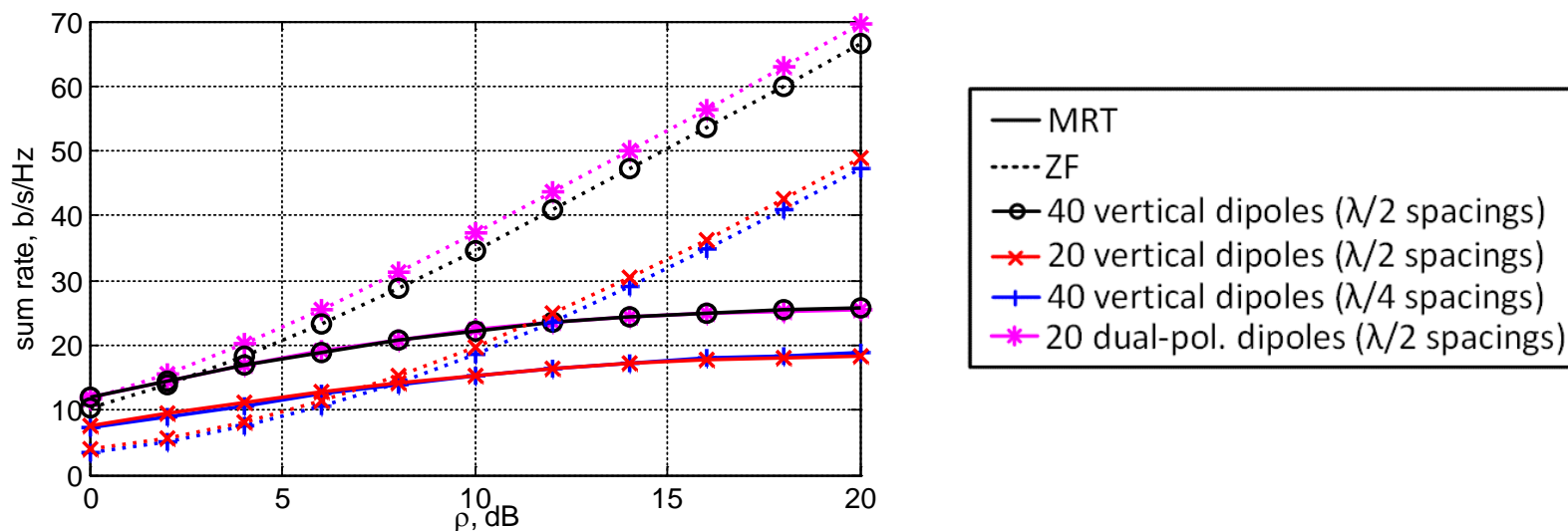
- Horizontal arrays of vertical dipoles at BS
- Vertical polarization of user terminals



Average sum rate is clearly degraded when inter-element spacing is reduced below  $\lambda/2$ -  $\lambda/3$  due to mutual coupling and limited aperture effects

- **Dual polarized arrays**

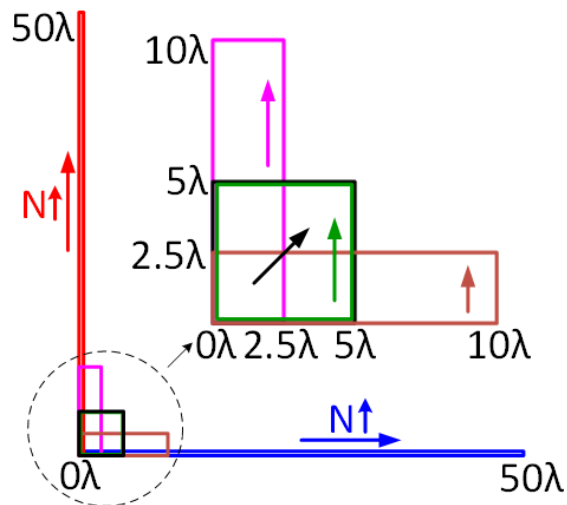
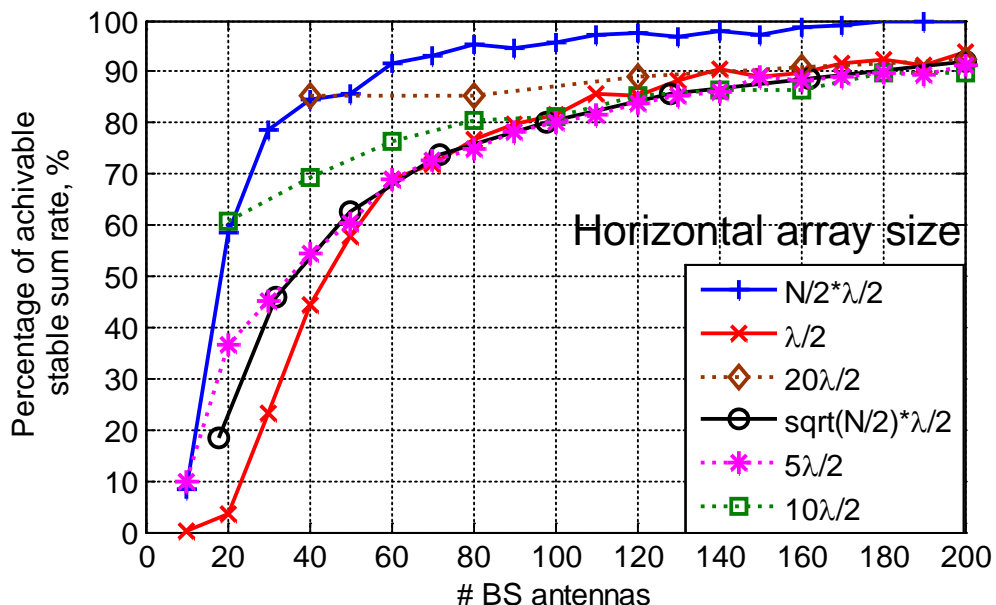
- Horizontal arrays of vertical dipoles or crossed-dipoles
- Random polarization of user terminals



- Dual-polarized arrays clearly surpass compact and single-polarized solutions.
- The benefits of using polarization diversity for reducing the polarization losses exceed the increased array gains provided by double-length single-polarized arrays

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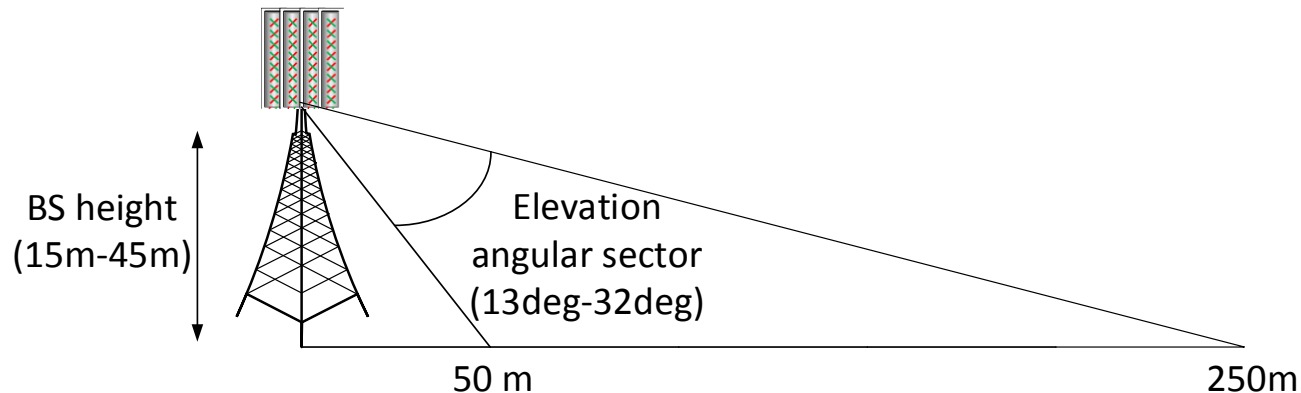
- Crossed dipole elements with inter-element distance of  $\lambda/2$
- ZF pre-coding and  $\rho=100/N$

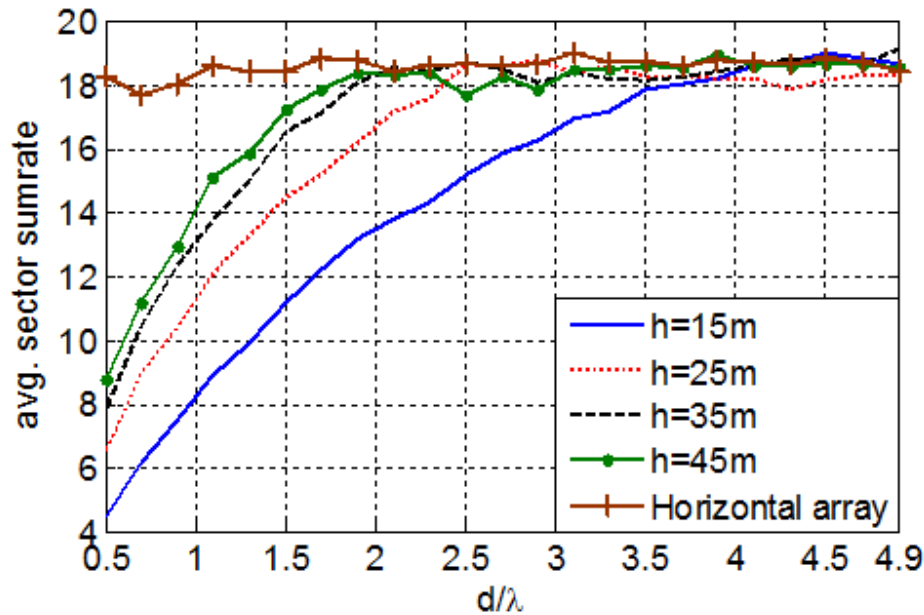


- Vertical beamforming allows reducing the horizontal size of the array but at the expense of increasing the number of elements.
- The reduced elevation angular sector limits the benefits of vertical beamforming.

# FD-MIMO with large spacings

- Inter-element distances beyond  $\lambda/2$  provide reduced beamwidths at the expense of the appearance of grating lobes
- **Which is the optimum spacing for elevation beamforming in FD-MIMO?**
- System model:
  - Vertical array with 16 antennas serving 4 users ( downlink)
  - Ideal Isotropic and uncoupled radiators
  - Free-space propagation
  - MRT precoding
  - $\rho=20\text{dB}$
  - Variable BS height  $\leftrightarrow$  variable elevation angular sector



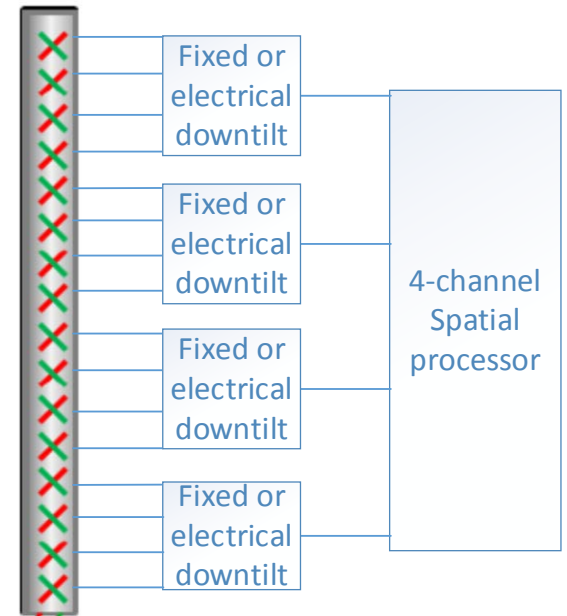
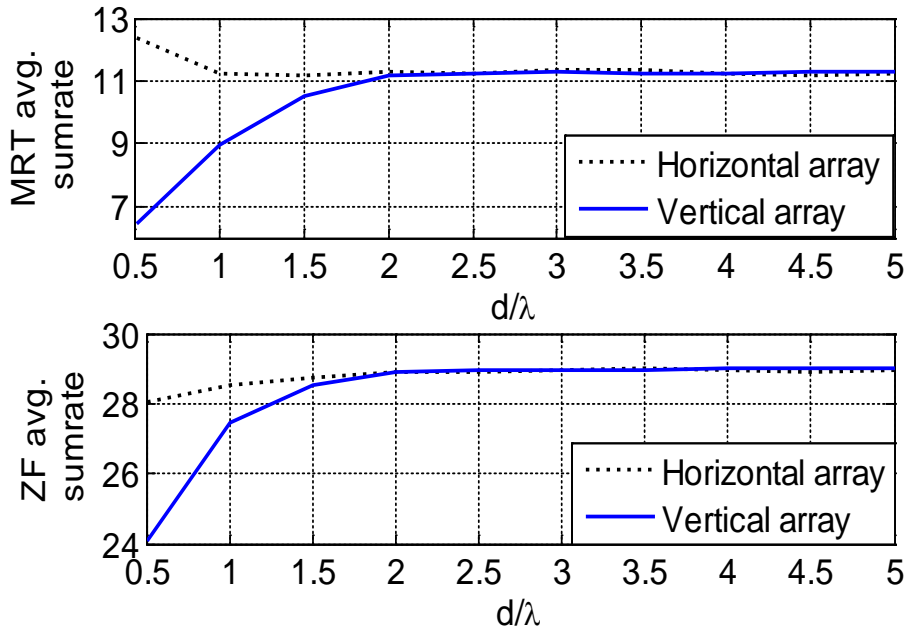


| BS height (m)    | Angular sector size (°) | Minimum antenna spacing creating grating lobes inside the sector of interest. (λ) |
|------------------|-------------------------|---|
| 15               | 13                      | 4.4   |
| 25               | 21                      | 2.9   |
| 35               | 27                      | 2.3   |
| 45               | 32                      | 2.1   |
| Horizontal array | 120                     | 0.6   |

- The directions of the grating lobes are calculated using:  $\theta_{GL} = \cos^{-1} \left( \pm \frac{m\lambda}{d} + \cos(\theta) \right)$
- Sumrate increases with antenna spacing until grating lobes start falling inside sector of interest.
- Beyond this optimum point, benefits of reduced beamwidth cancel out with the appearance of grating lobes.



- BS height is set to 25m
- Linear arrays of 16 antenna elements formed by 8 pairs of 45° slanted cross-dipoles backed by a perfect conductor.
- K=4 user terminals with random polarization



- Hybrid analog/digital beamforming array solution can reduce the effects of GL out of the sector of interest

- Mutual coupling does not allow reducing the inter-element spacing below  $\lambda/2$ -  $\lambda/4$  (depending on the scenario and the radiating elements).
- Polarization diversity provides better performance than reducing inter-element spacing.
- Polarization diversity provides better performance than using single polarization and doubling the size of the array.
- Elevation beamforming in FD-MIMO allows reducing the horizontal size of the array at the expense of the need of more antennas.
- Elevation beamforming is limited by reduced angular elevation sector.
- Optimum vertical element separation is the larger one for which the grating lobes still do not fall inside the sector of interest.



***Thanks for your kind attention!***

- Questions?

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